

AMENDMENTS TO THE SPECIFICATION:

Before the paragraph beginning at page 1, line 4,
insert the following:

--REFERENCE TO COMPUTER PROGRAM LISTINGS

A computer program listing appendix with twelve files is provided on a compact disc as part of the invention disclosure. The material of the twelve files on the compact disc is incorporated by reference. The files included on the compact disc are:

- generate-discretization.mu has a size of 6,241 bytes and was created (stored on the CD-R) on December 12, 2006.

This file contains the program "generate-discretization", referred to as Appendix 1.

- preparations.mu has a size of 3,101 bytes and was created (stored on the CD-R) on December 12, 2006. This file contains the subroutine "preparations", referred to as Appendix 2.

- setup-equations.mu has a size of 17,414 bytes and was created (stored on the CD-R) on December 12, 2006.

This file contains the subroutine "setup-equations", referred to as Appendix 3.

- solve-equations.mu has a size of 4,681 bytes and was created (stored on the CD-R) on December 12, 2006. This file contains the subroutine "solve-equations", referred to as Appendix 4.

- analyze-solution.mu has a size of 22,654 bytes and was created (stored on the CD-R) on December 12, 2006. This file

contains the subroutine "analyze-solution", referred to as

Appendix 5.

- appendix6.txt has a size of 10,588 bytes and was created (stored on the CD-R) on December 12, 2006. This file contains the output for D100, Order 2, on the grid $(-1,1)^3$, optimize=0, referred to as Appendix 6.
- appendix7.txt has a size of 3,289 bytes and was created (stored on the CD-R) on December 12, 2006. This file contains the output for D100, Order 2, on the grid $(-1,1)^3$, optimize=1, referred to as Appendix 7.
- appendix8.txt has a size of 9,465 bytes and was created (stored on the CD-R) on December 12, 2006. This file contains the output for D100, Order 2, on the grid $(-1,1)^3$, optimize=2, referred to in the following as Appendix 8.
- appendix9.txt has a size of 47,206 bytes and was created (stored on the CD-R) on December 12, 2006. This file contains the output for D100, Order 4, on the grid $(-2,2)^3$, optimize=0, 30, referred to as Appendix 9.
- appendix10.txt has a size of 4,092 bytes and was created (stored on the CD-R) on December 12, 2006. This file contains the output for D100, Order 4, on the grid $(-2,2)^3$, optimize=1, referred to as Appendix 10.

- appendix11.txt has a size of 49,617 bytes and was created (stored on the CD-R) on December 12, 2006. This file contains the output for D100, Order 4, on the grid $(-2, 2)^3$, optimize=2, 5, referred to as Appendix 11.
- appendix12.txt has a size of 16,572 bytes and was created (stored on the CD-R) on December 12, 2006. This file contains the output for D200, Order 2, on the grid $(-1, 1)^3$, optimize=0, referred to as Appendix 12.--

Please replace the paragraph spanning pages 8 and 9 with the following:

--An example is a general one-dimensional discretization for a derivative at node i which uses the stencil between the nodes $i - m$ and $i + n$, where m and n are given positive integers. On the stencil $S = (i - m, i - m + 1, \dots, i - 1, i, i + 1, \dots, i + n - 1, i + n)$, the approximation of the first derivative can be written as

$$u_x = \frac{1}{\Delta x} \{ a_{-m} u_{i-m} + a_{-m+1} u_{i-m+1} + \dots + a_{-1} u_{i-1} + a_0 u_i + a_1 u_{i+1} + \dots + a_{n-1} u_{i+n-1} + a_n u_{i+n} \}.$$

(1)

The coefficients $a_j, i = j \in S$ determine the numerical properties of the discretization.

A general description of the above discretization can be found in D1 which discusses the method for obtaining the coefficients a_j . Expression (1) also generalizes to higher derivatives. --

Replace the paragraph beginning at page 47, line 16 with the following:

--The second derivative $D_2 = \frac{\partial^2 u}{\partial e_1^2}$ can be expressed in the grid-based derivatives $u_{xx}, u_{yy}, u_{zz}, u_{xy}, u_{yz}$ and u_{zx} according to

$$\frac{\partial^2 u}{\partial e_1^2} = \cos^2 \alpha \cos^2 \beta \frac{\partial^2 u}{\partial x^2} + \sin^2 \alpha \cos^2 \beta \frac{\partial^2 u}{\partial y^2} + \sin^2 \beta \frac{\partial^2 u}{\partial z^2} + 2 \cos \alpha \cos^2 \beta \sin \alpha \frac{\partial^2 u}{\partial x \partial y} + 2 \cos \alpha \cos \beta \sin \beta \frac{\partial^2 u}{\partial x \partial z} + 2 \sin \alpha \cos \beta \sin \beta \frac{\partial^2 u}{\partial y \partial z} \quad (21)$$

The terms $T_{xx}, T_{xy}, T_{xz}, T_{yy}, T_{yz}$ and T_{zz} are obtained by the computer program mentioned before, and are given in appendix 12. The stencils $T_{xx}, T_{xy}, T_{xz}, T_{yy}, T_{yz}$ and T_{zz} have been added in various quantities to the stencils $Tf_{xx}, Tf_{xy}, Tf_{xz}, Tf_{yy}, Tf_{yz}$ and Tf_{zz} to obtain the more symmetric representation of equation 20. This shows once more the use of the degrees of freedom, and the equivalence between two expressions for an approximation of D_p using a different Tf but sharing the basis described by the stencils.--

Replace the list of symbols beginning on page 54 with the following:

--List of symbols

- A an amplitude of a Fourier component
- A', A'' intermediate bases in the transformation from the grid basis to the local basis B
- a, b, c, \dots components of the vector \vec{a}
- \vec{a} vector of preferential direction
- $B(\vec{e}_1, \vec{e}_2, \vec{e}_3, \dots)$ a local basis, with \vec{e}_1 along a preferential direction, i.e. $\vec{e}_1 // \vec{a}$
- C_c computational coefficients used in the approximation of D_p^A , which are dependent on the numerical formulation used
- C_s computational coefficients used in the approximation of D_p^A , in the Finite Difference formulation ; weighting coefficients the weighting coefficients C_s for node l, m, n, \dots
- $C_{l,m,n,\dots}$
- D_p spatial p^{th} derivative, to be discretized
- D_p^A an approximation to D_p
- D_p^{LC} an approximation to D_p in the Finite Difference formulation, representing a linear combination of values

$D_p^{\alpha_i}$	an approximation to D_p in the Distribution Method, depending on the distribution coefficients α_i
$D_p^{\varphi,\psi}$	an approximation to D_p in the Finite Element formulation depending on the basis function φ and the test function ψ
f	the flux
I	the imaginary unit, such that $I^2 = -1$
i, j, k, \dots	indices numbering the nodes of a structured grid
$i_{\max}, j_{\max}, k_{\max}$	maximum indices of a grid
I_{el}	the integral of the derivative D_p over a volume, used in the Residual Distribution Method
M	order of the error of a discretization
N	number of dimensions
P	the point where the derivative is computed
p	index for a higher (p^{th}) derivative, or first derivative ($p = 1$)
p_1, p_2, p_3, \dots	the powers of the derivatives with respect to $\vec{e}_1, \vec{e}_2, \dots$ in a mixed derivative
q_1, q_2, q_3, \dots	arbitrary variables
r	an integer summation index
r_{\max}	the maximum value of r in the summation
S	the stencil : the set of points used in the computation of the approximation D_p^A
t	the time coordinate
$t_{11}, t_{1,2}, \dots$	coefficients used in the transformation between coordinate systems
T_β	represent the terms in the discretization β resulting from degrees of freedom which remain when the approximated value D_p^A is optimized
u	unknown at a grid point
u_s	unknown at a point of the stencil S
u_α	derivative of u with respect to α , e.g. $u_\alpha = \frac{\partial u}{\partial \alpha}$
\vec{x}	N -dimensional position vector
$\vec{\nabla}$	differential operator, $\left(\frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z}, \dots\right)^T$

α_i the distribution coefficient used in the Distribution Method
for the distribution of the part $\alpha_i I_{el}$ or $\alpha_i f$ to node i

$\Delta x, \Delta y, \Delta z, \dots$ the mesh spacings in the coordinate directions

Δt the time increment

$\frac{\partial u}{\partial x}$ partial p^{th} derivative with of u with respect to x

$\frac{\partial^p}{\partial x^p}$ derivative with respect to x

ε_n error term in D_p^A

ε_s error term in the expression of u_s using a truncated
Taylor series expansion

$\vec{\kappa}$ the wave number vector

φ the basis function used in the Finite Element method for repre-
senting u over the element

ψ test function used in the integrals of the derivative in the Finite
Element formulation

ω the angular frequency--